



# VAQEM: A Variational Approach to Quantum Error Mitigation

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**IBM:** Nate Earnest-Noble, Ali Javadi-Abhari

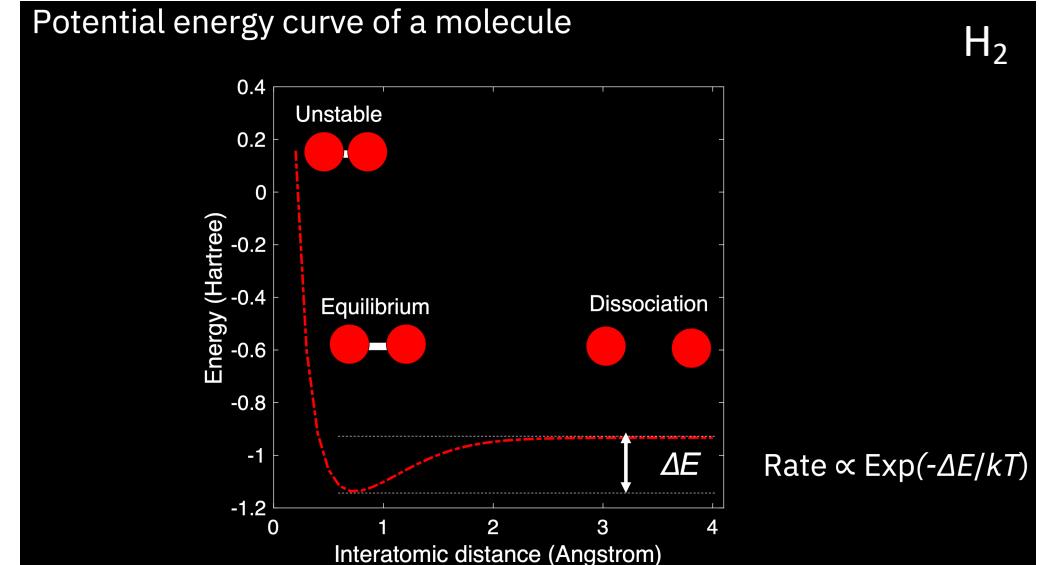
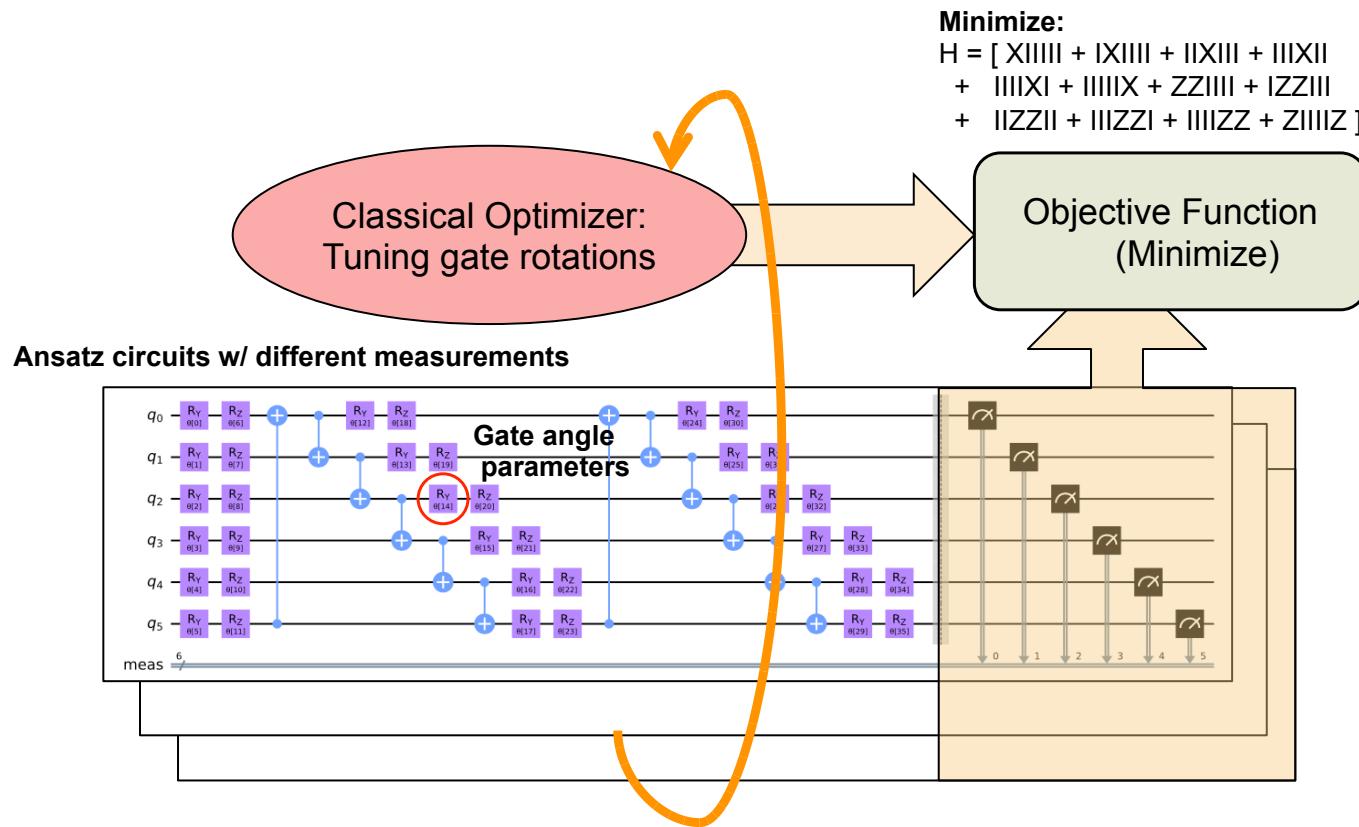
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CIFellows (NSF 2030859) and IBM/CQE.

# Summary: A variational approach to quantum error mitigation

- **Background:** VQAs are considered suitable to the NISQ era, but machine fidelity is still too low for real world applicability.
- **Goal:** Apply error mitigation in an optimal manner to VQAs for max fidelity – but this is challenging as device and circuit complexity increase.
- **Proposal:**
  - Integrate EM techniques into VQA's framework of iterative parameter tuning: enabling a feedback-based approach towards optimal EM for the application / device.
  - Targets two idle-time EM methods: insertion of dynamical decoupling sequences and single-qubit gate scheduling.
- **Result:** Improves the quality of the VQA measured objective by 3x on average.

# Variational Quantum Algorithms

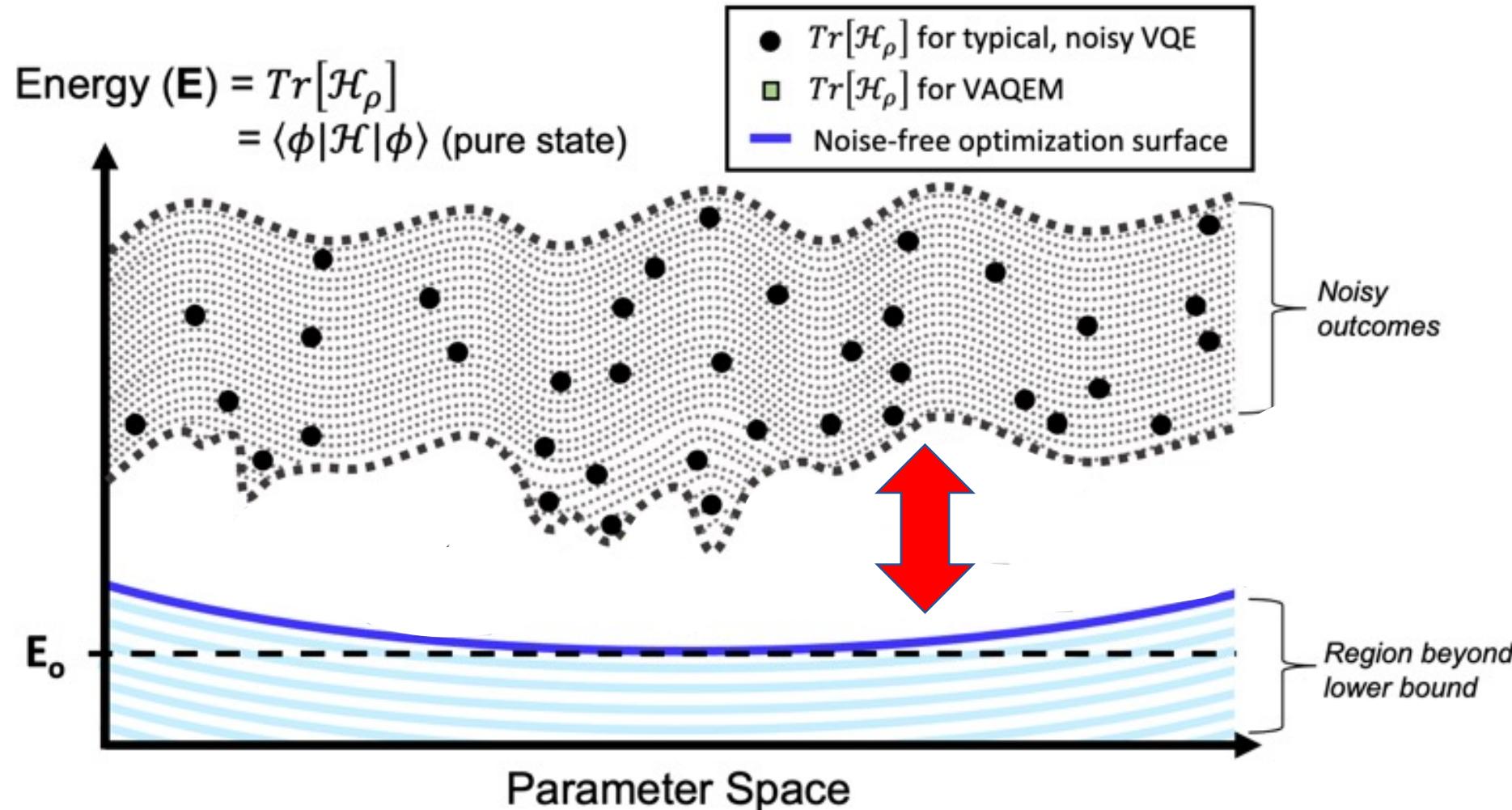


Variational principle: the energy of any trial wave-function is greater than or equal to the exact ground state energy

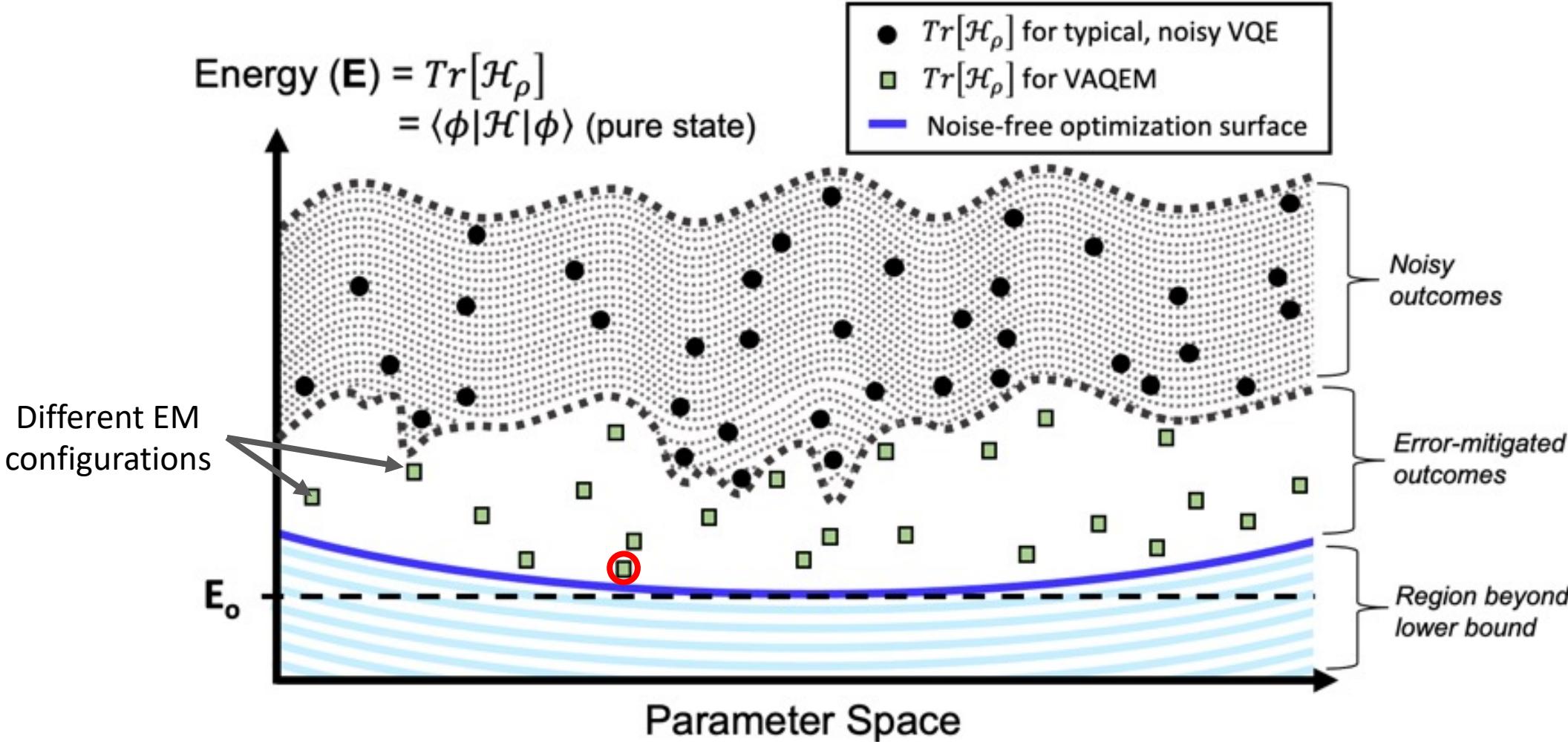
$$\frac{\langle \Psi(\vec{\theta}) | H | \Psi(\vec{\theta}) \rangle}{\langle \Psi(\vec{\theta}) | \Psi(\vec{\theta}) \rangle} \geq E_G$$

<https://qiskit.org/learn/intro-qc-qh/>

# VQA Fidelity in the NISQ era

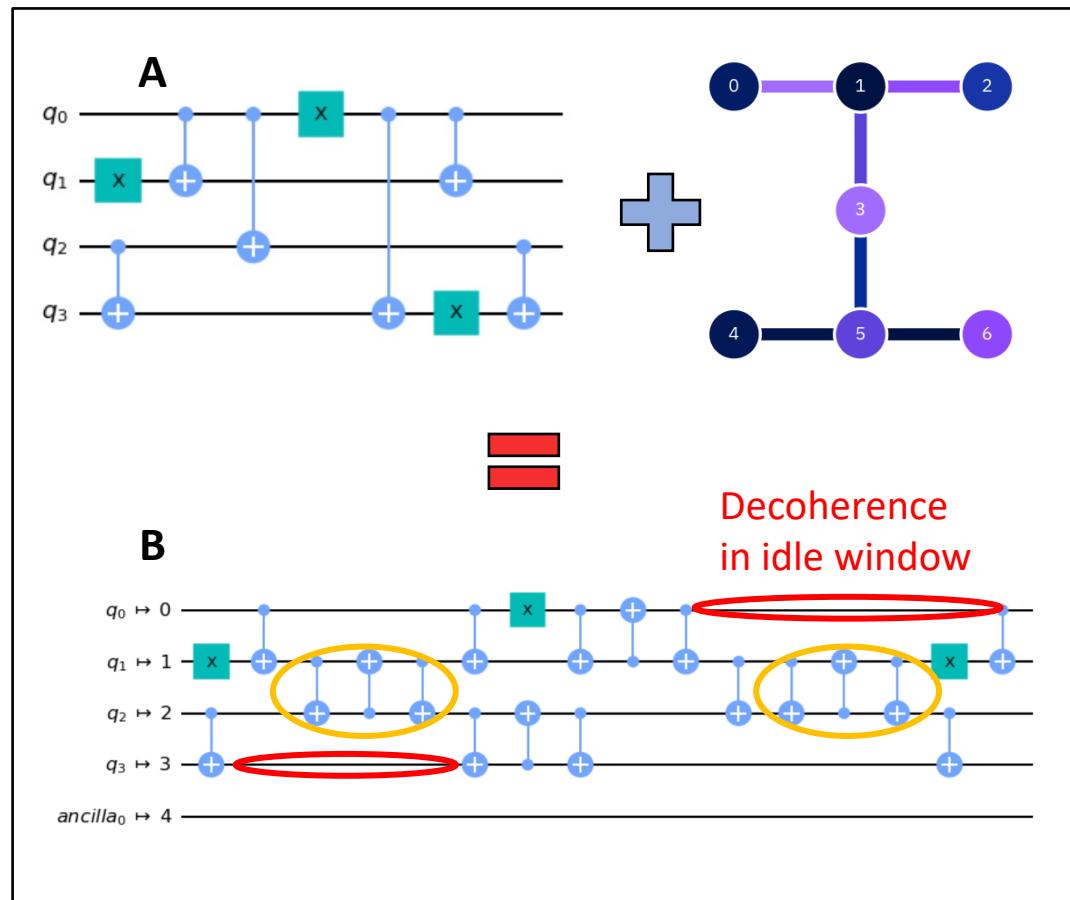


# Impact of Error Mitigation

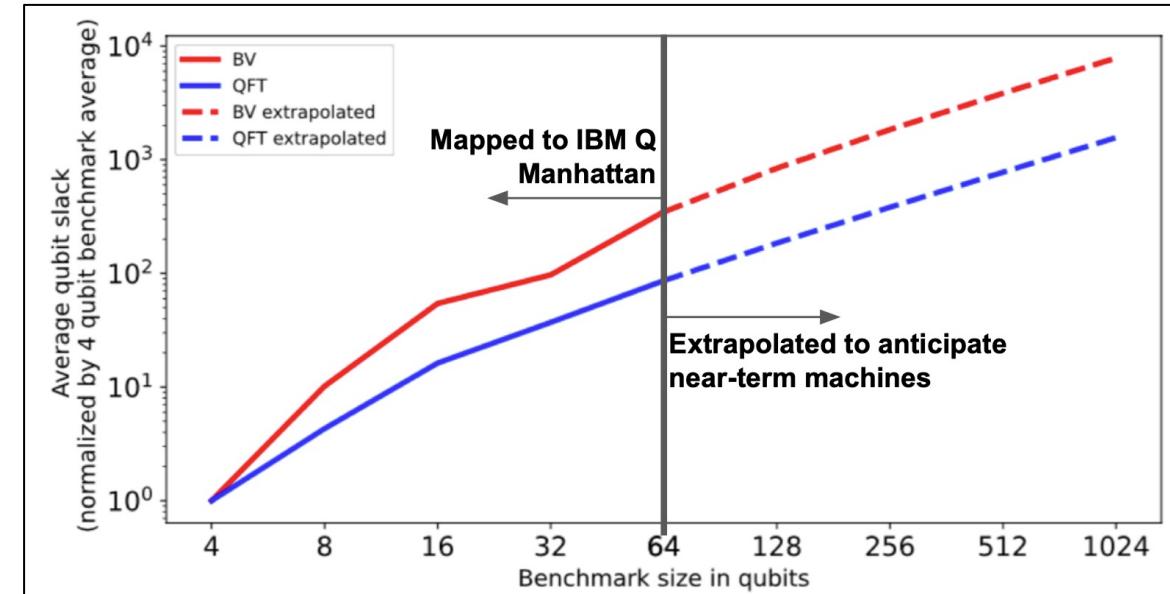


# EM targeting QC Idle windows

*Compiling for machines with limited connectivity  
leads to increased depth and long critical paths*

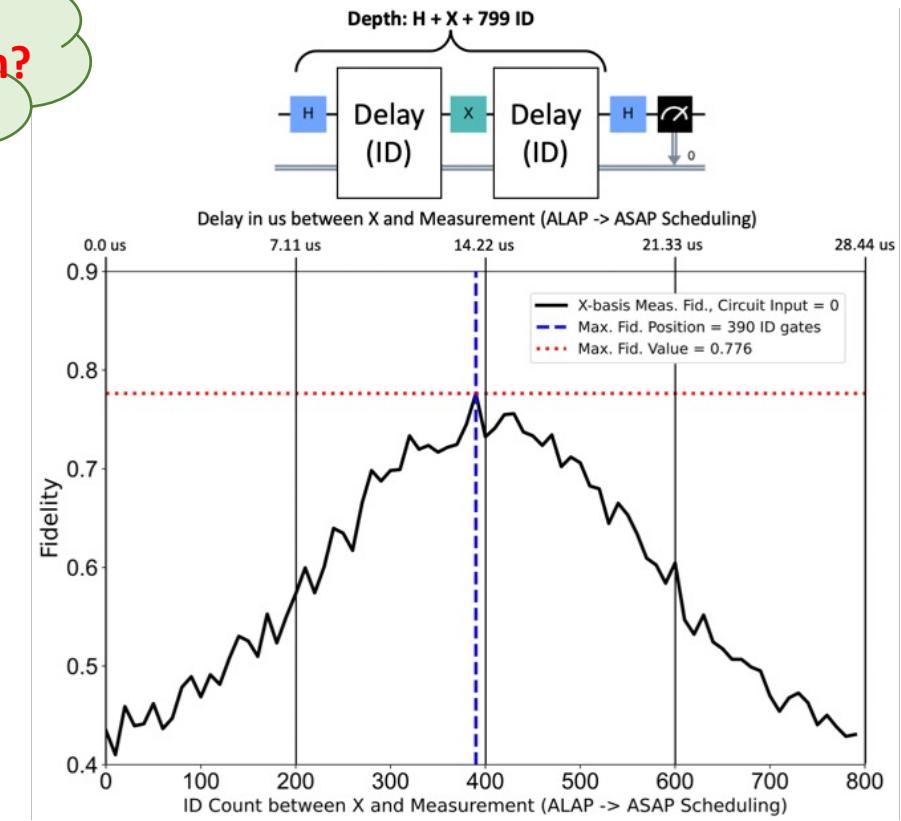
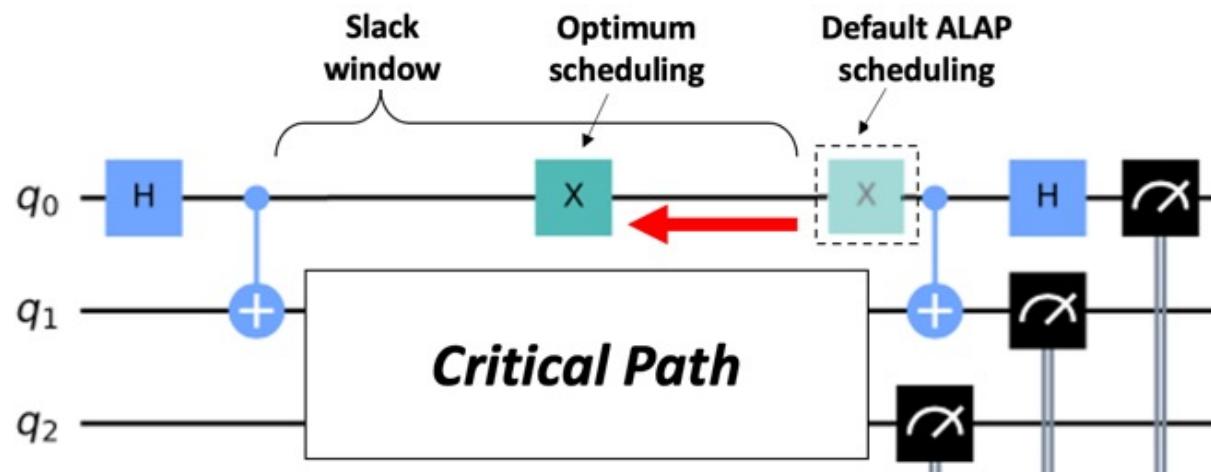


*As application sizes increases, path lengths become longer and more diverse leading to more slack*



# Idle Window Signal Refocusing: 1Q gate scheduling

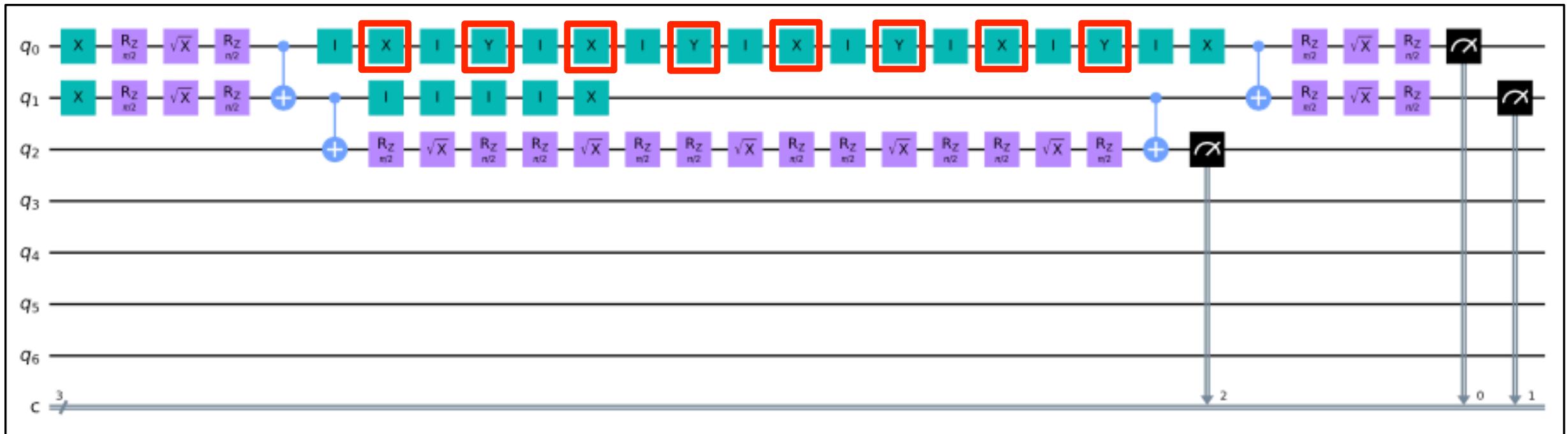
Spin Echo Correction: Details in the paper!



# Idle Window Signal Refocusing: Dynamic decoupling

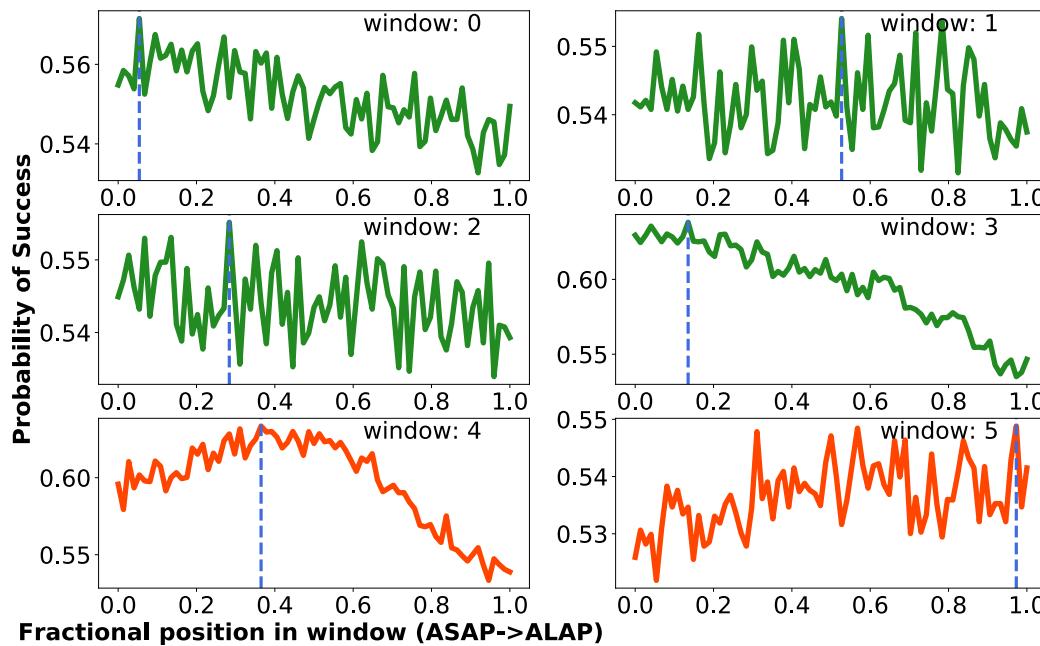
Spin Echo Correction: Details in the paper!

optimal gate types /  
number / spacing ?

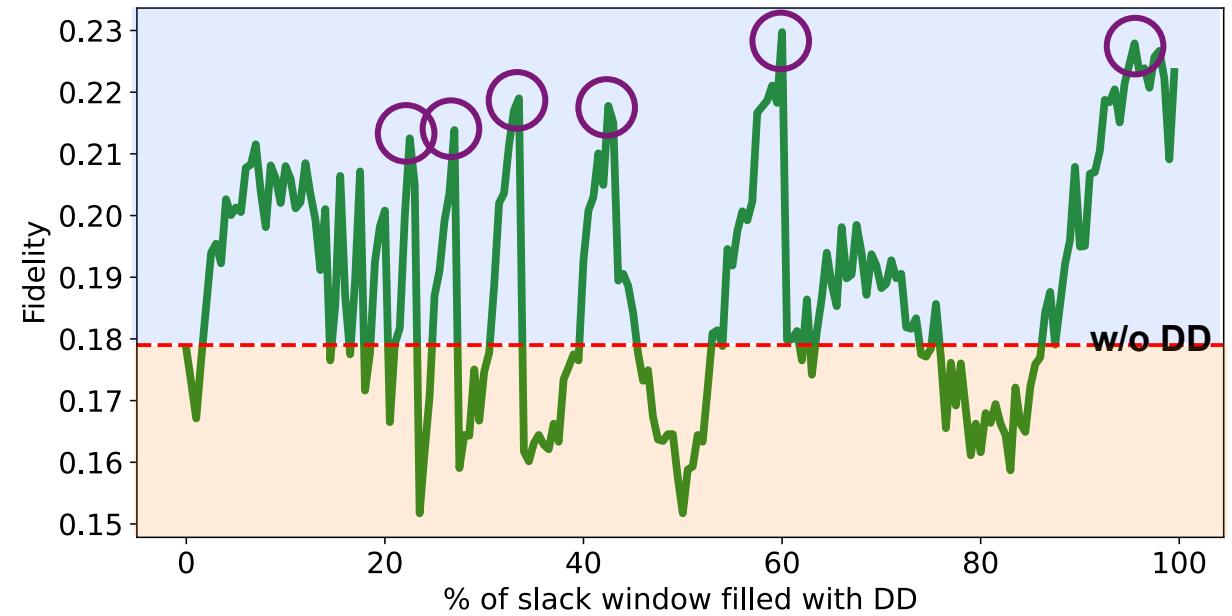


# Optimizing EM: practical challenges

**1) Imperfect knowledge of stimuli and their effects makes theory driven EM heuristics less effective.**



1q gate scheduling



DD insertion

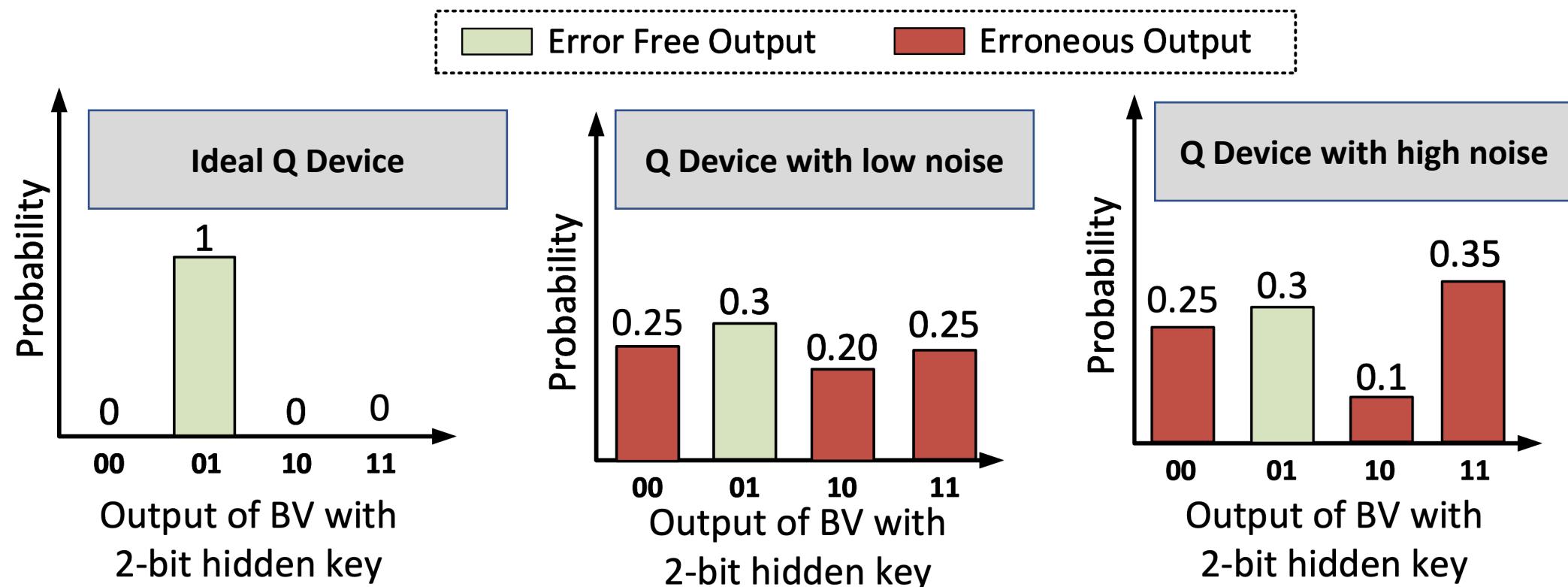
# Optimizing EM: practical challenges

**2) Micro-analyzing stimuli effects for every EM instance is not scalable.**



# Optimizing EM: practical challenges

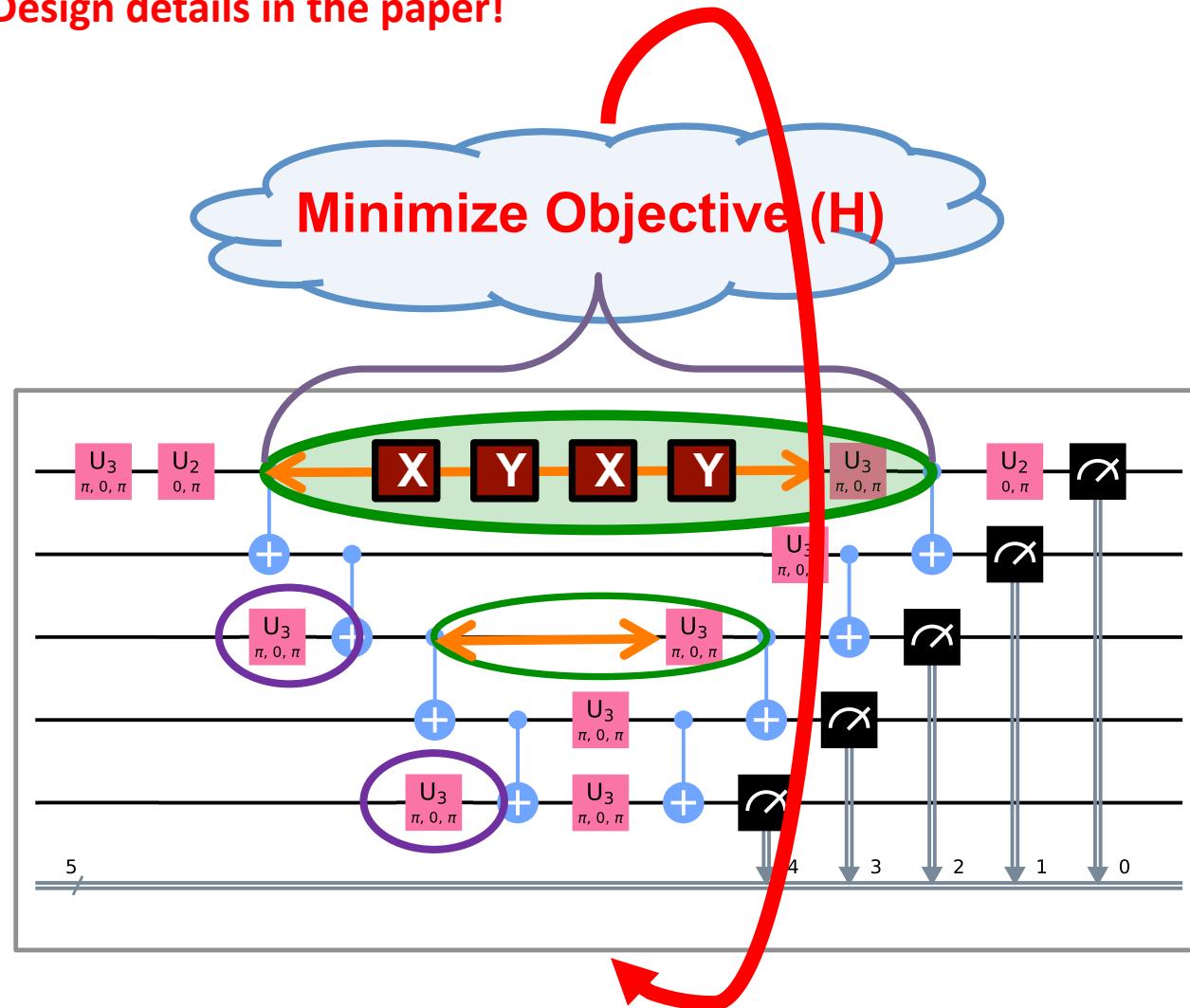
3) Stimuli-agnostic outcome driven approaches are not always possible since outcomes are often unknown and usually not of highest probability.



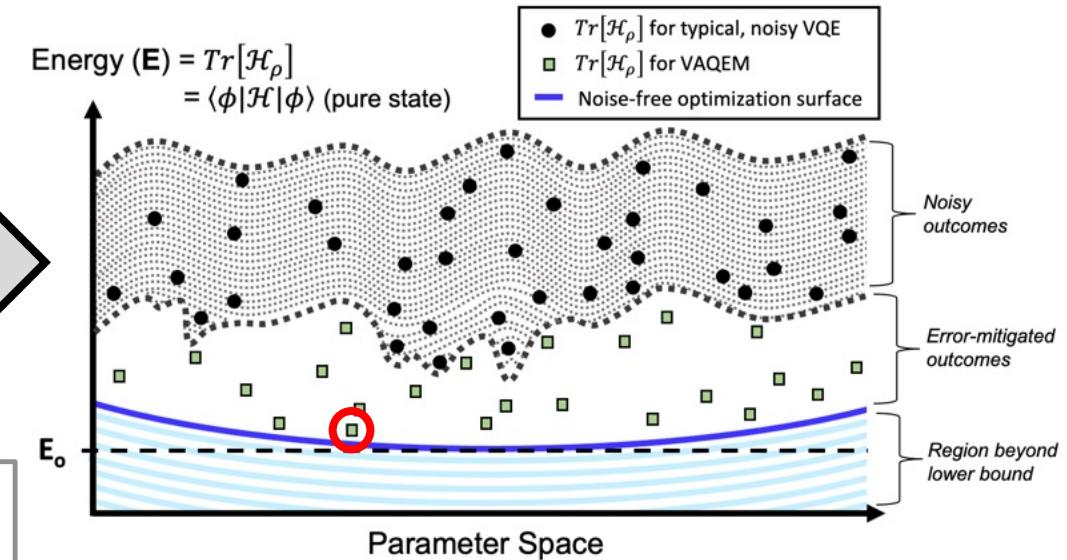
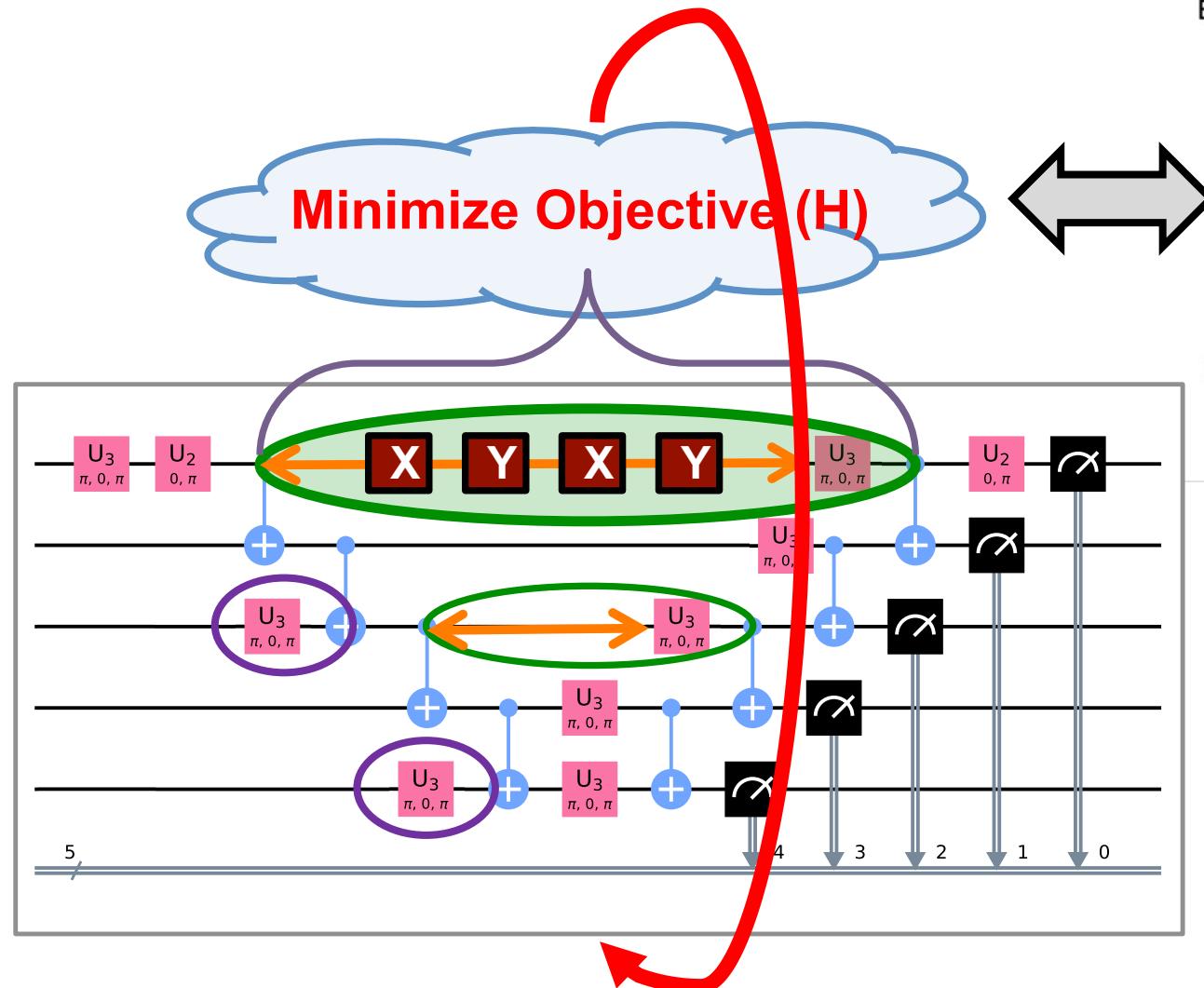
\* Ensemble of Diverse Mappings MICRO2019

# VAQEM: Tuning EM features in the VQA setting

Design details in the paper!



# VAQEM: Tuning EM features in the VQA setting

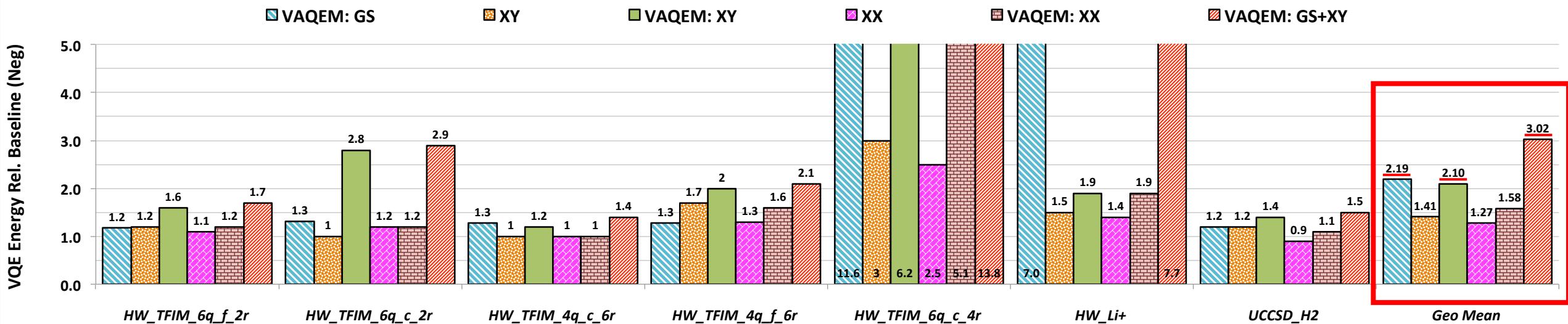


$$\frac{\langle \Psi(\vec{\theta}) | H | \Psi(\vec{\theta}) \rangle}{\langle \Psi(\vec{\theta}) | \Psi(\vec{\theta}) \rangle} \geq E_G$$

Only \*quantum\* EM –  
details in the paper!

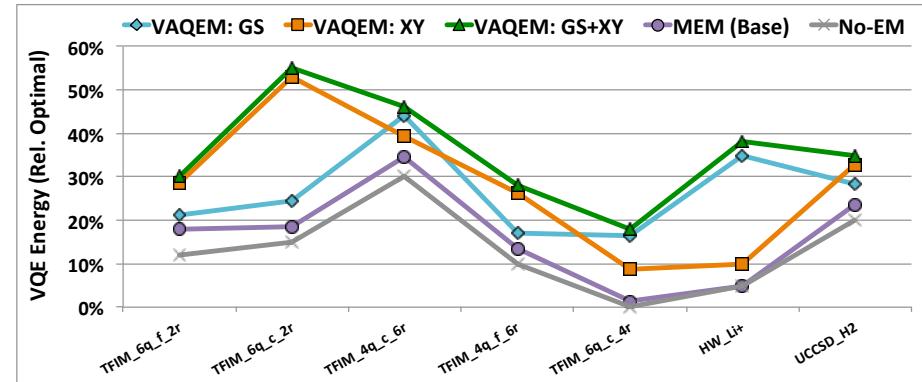
# VQE benefits from VAQEM I

Bench	<b>6q/f/2r</b>	<b>6q/c/2r</b>	<b>4q/c/6r</b>	<b>4q/f/6r</b>	<b>6q/c/4r</b>	<b>Li+</b>	<b>H2</b>
<b>Depth</b>	54	31	57	101	55	90	61
<b># Win</b>	42	24	22	34	30	45	26

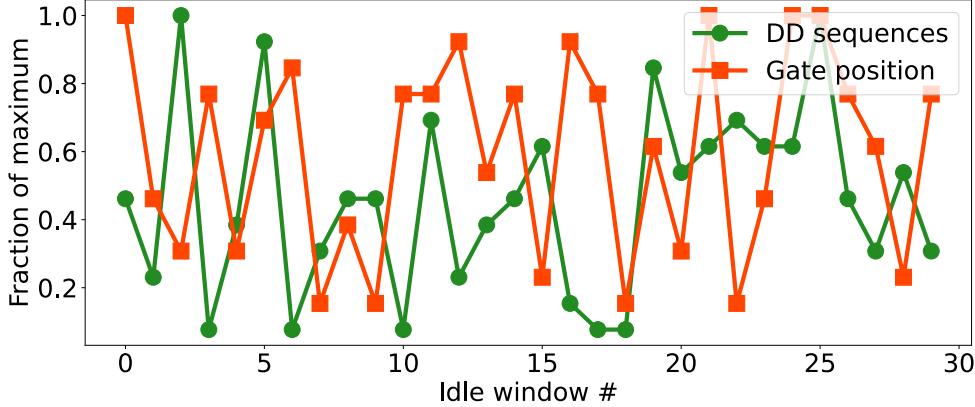


# More in the paper:

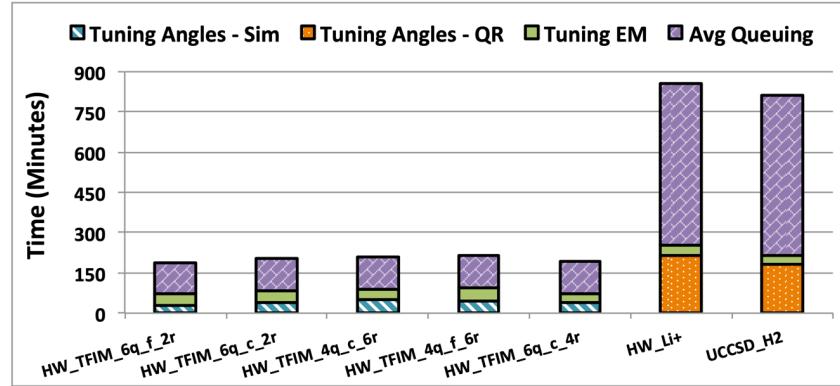
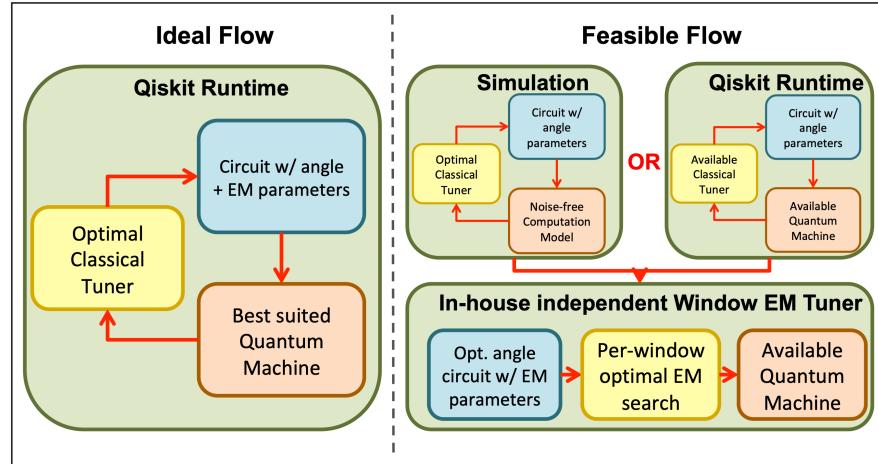
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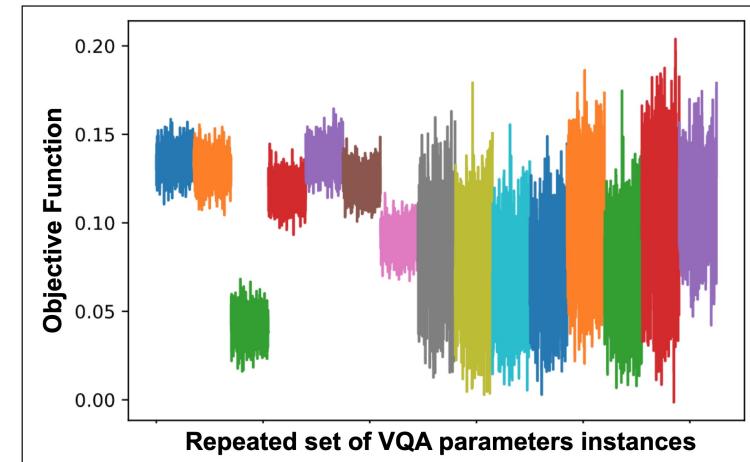
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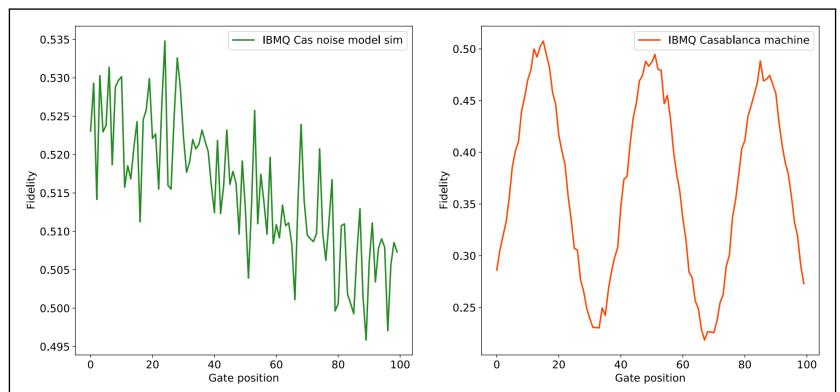
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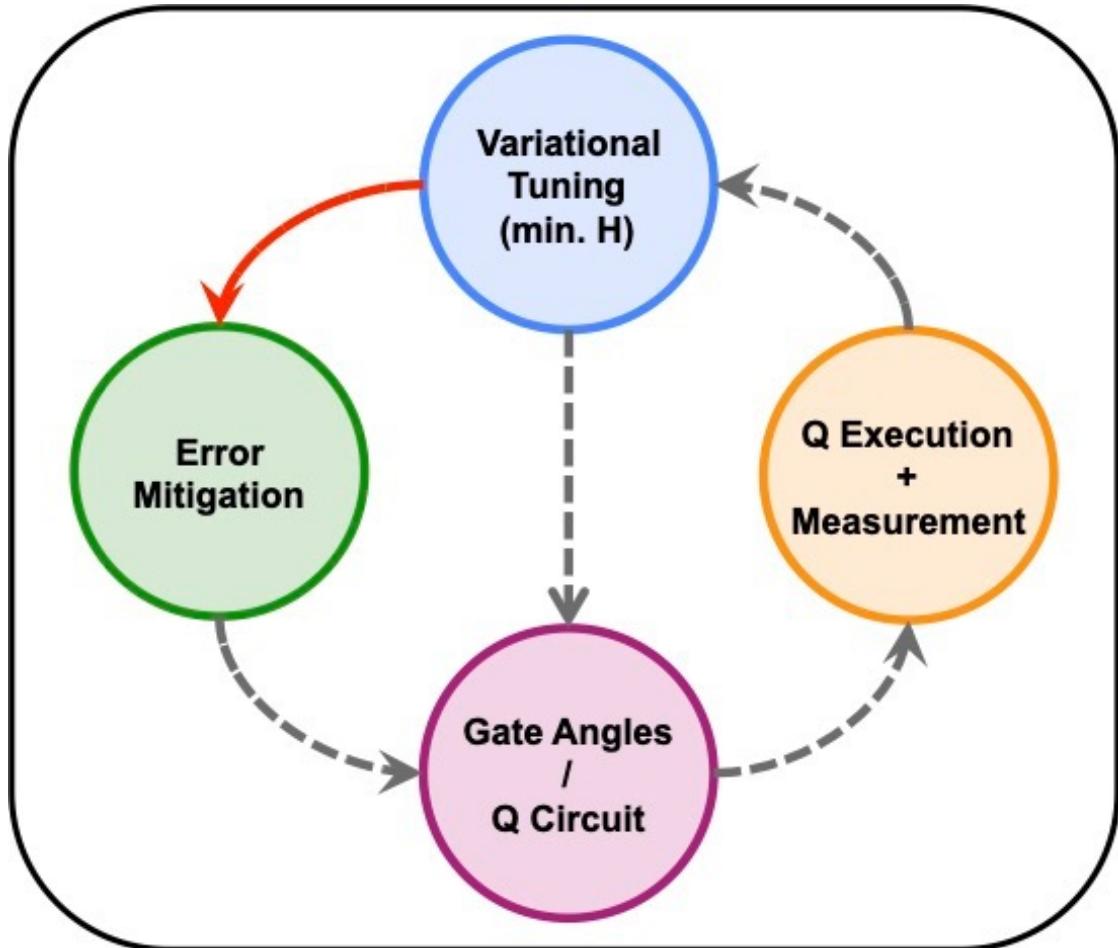


5



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# Conclusion: A variational approach to quantum error mitigation



## Future Directions:

- Variationally tune more features of current EM techniques
- Integrate more EM techniques into the VAQEM framework
- Explore tunable optimizations outside of error mitigation

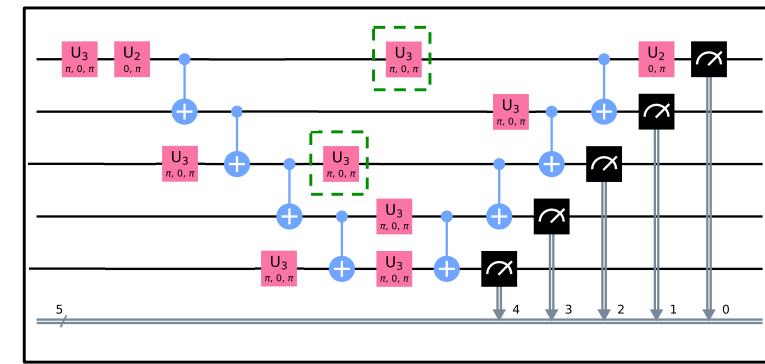
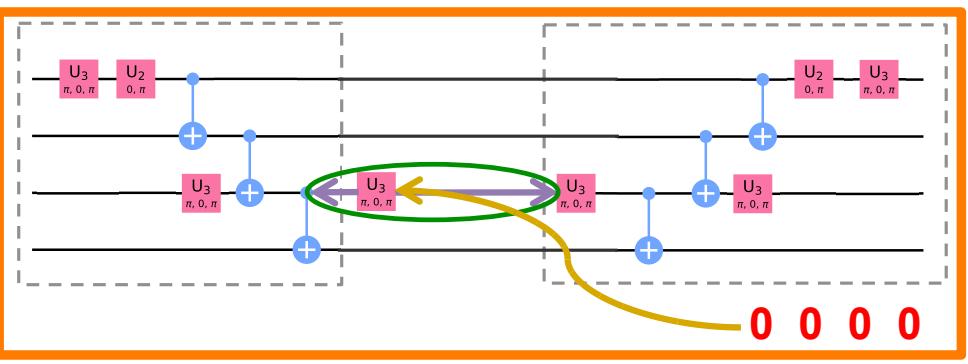
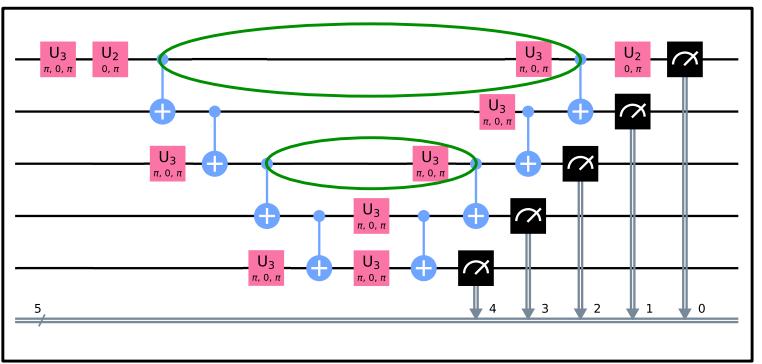
# Thank you!

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VAQEM: [arXiv:2112.05821](https://arxiv.org/abs/2112.05821)

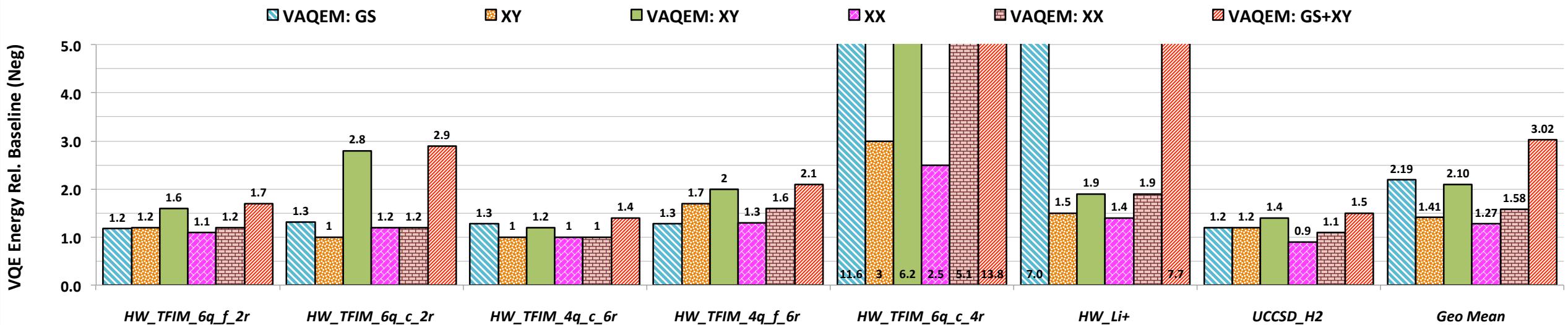
TimeStitch: [arXiv:2105.01760](https://arxiv.org/abs/2105.01760)

# Backup

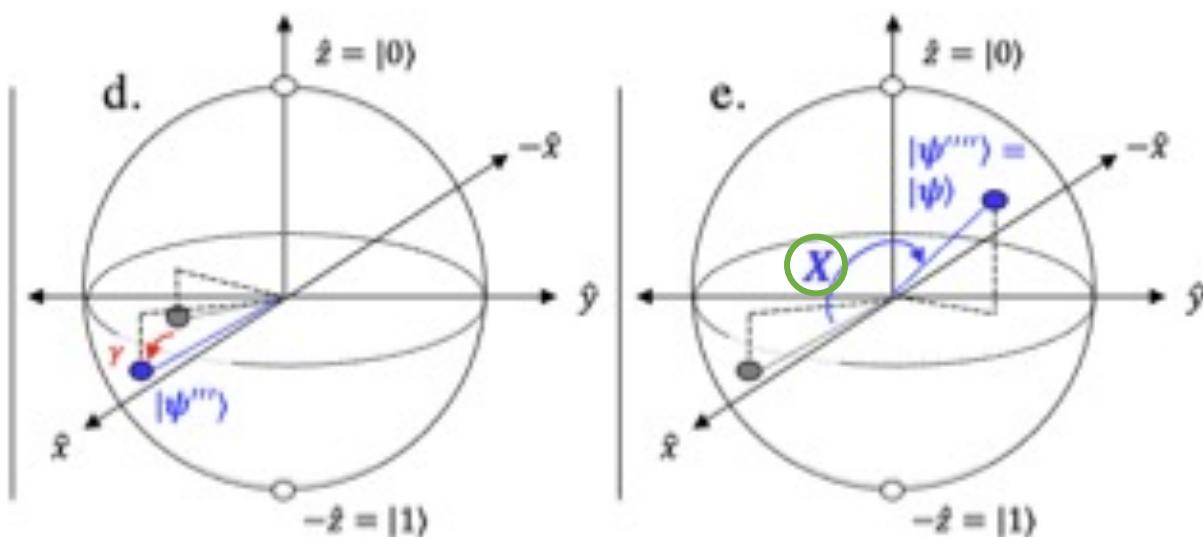
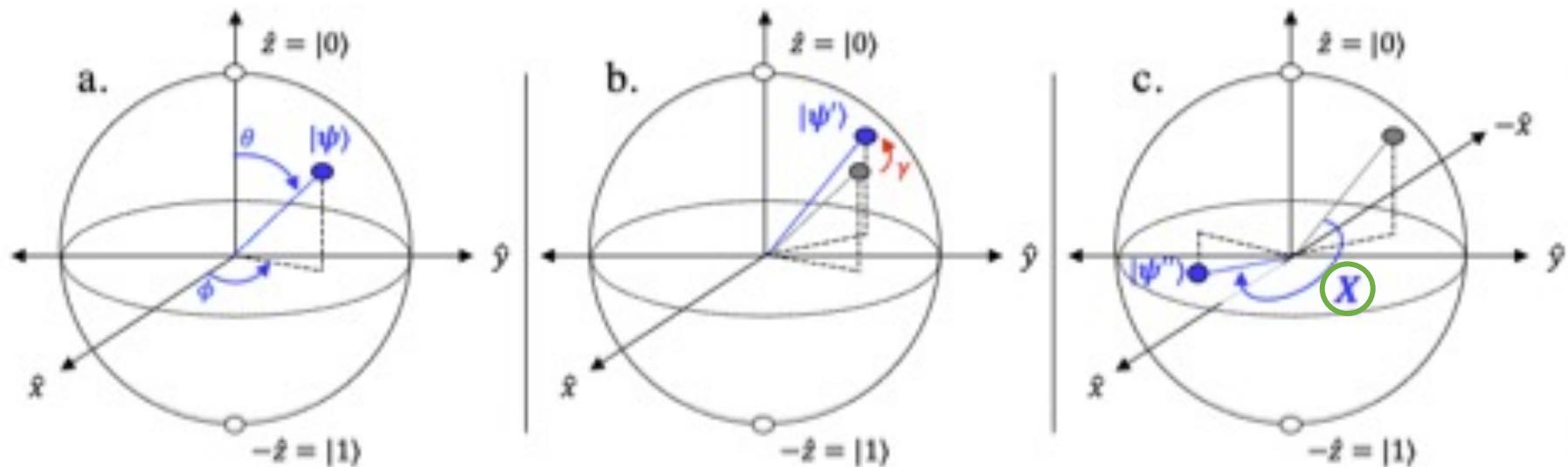


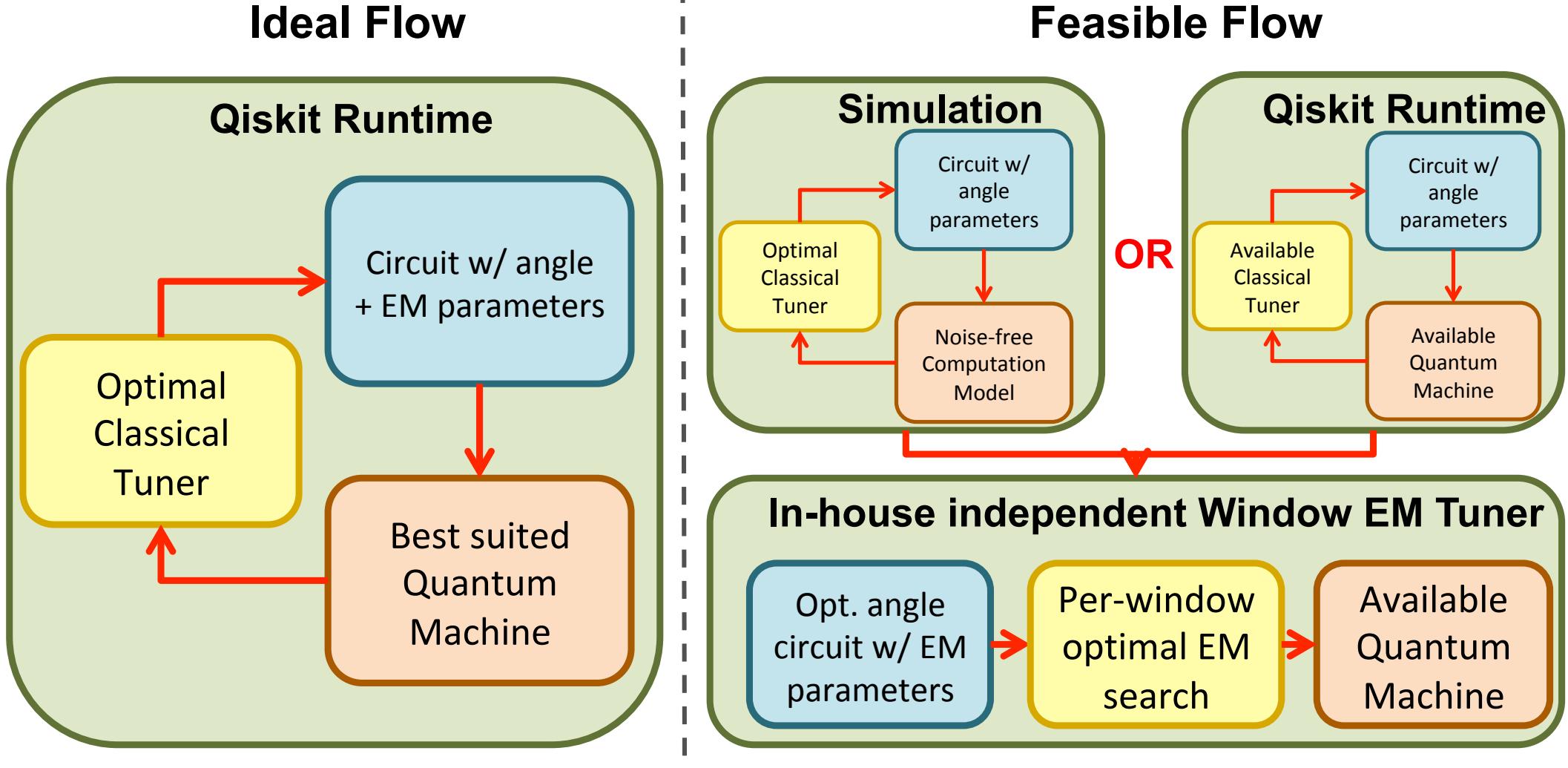
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# EM inspired by spin echo correction



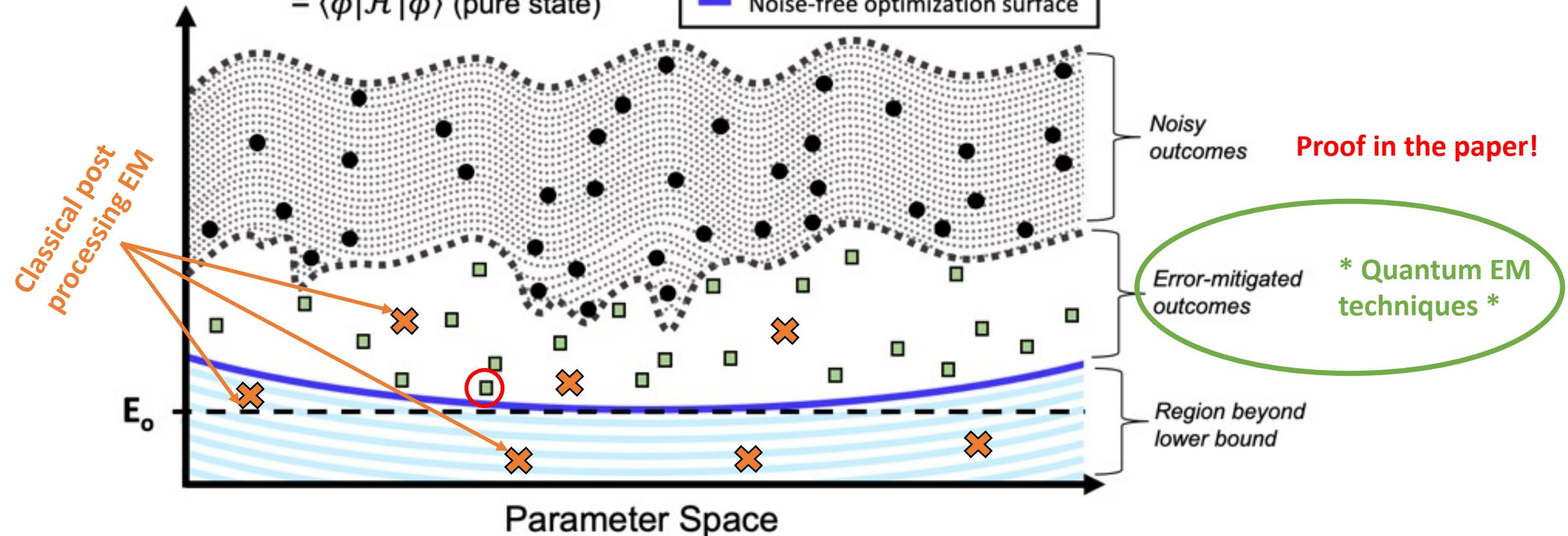


# Tunable Error Mitigation Scope

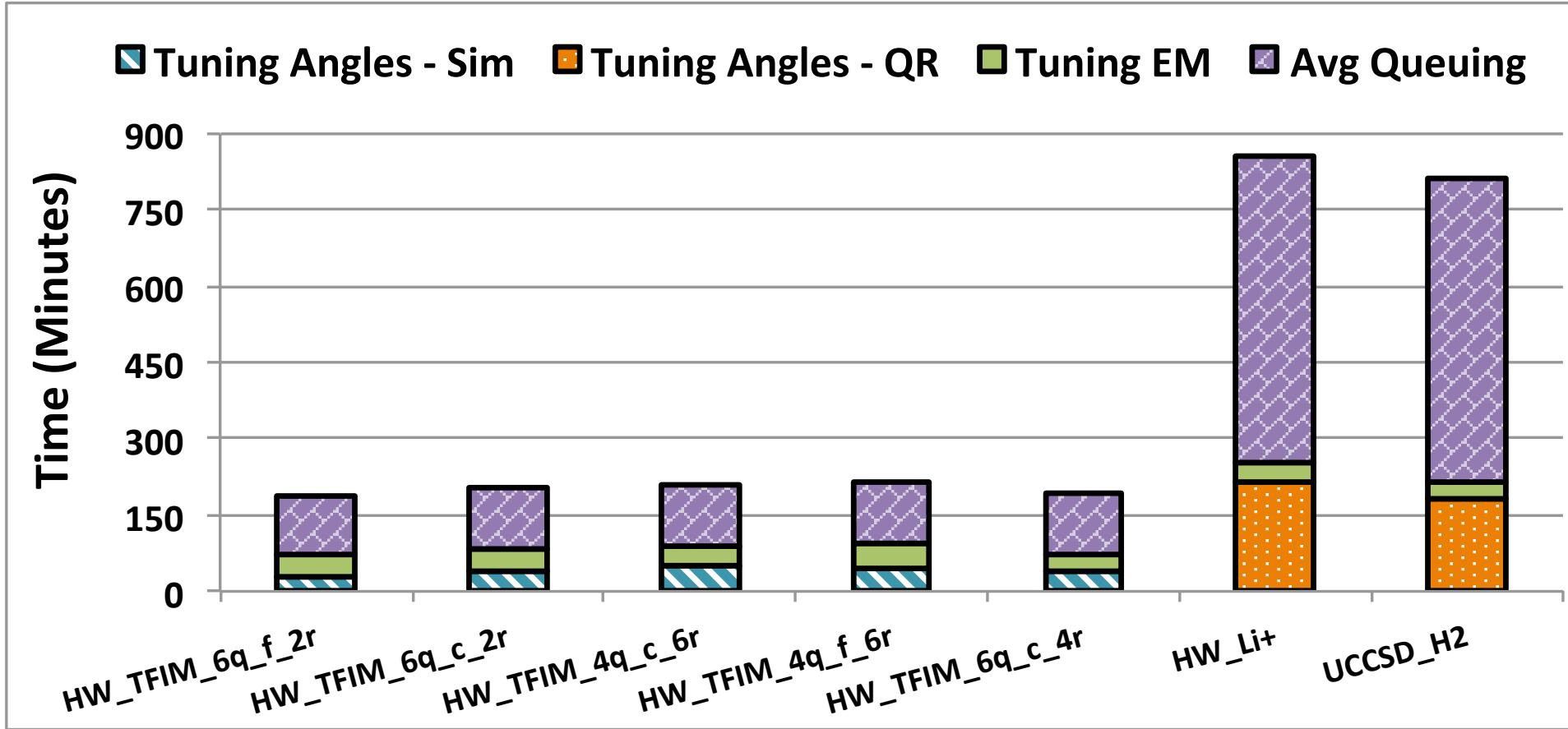
$$\begin{aligned} \text{Energy (E)} &= \text{Tr}[\mathcal{H}_\rho] \\ &= \langle \phi | \mathcal{H} | \phi \rangle \text{ (pure state)} \end{aligned}$$

- $\text{Tr}[\mathcal{H}_\rho]$  for typical, noisy VQE
- $\text{Tr}[\mathcal{H}_\rho]$  for VAQEM
- Noise-free optimization surface

$$\frac{\langle \Psi(\vec{\theta}) | H | \Psi(\vec{\theta}) \rangle}{\langle \Psi(\vec{\theta}) | \Psi(\vec{\theta}) \rangle} \geq E_G$$

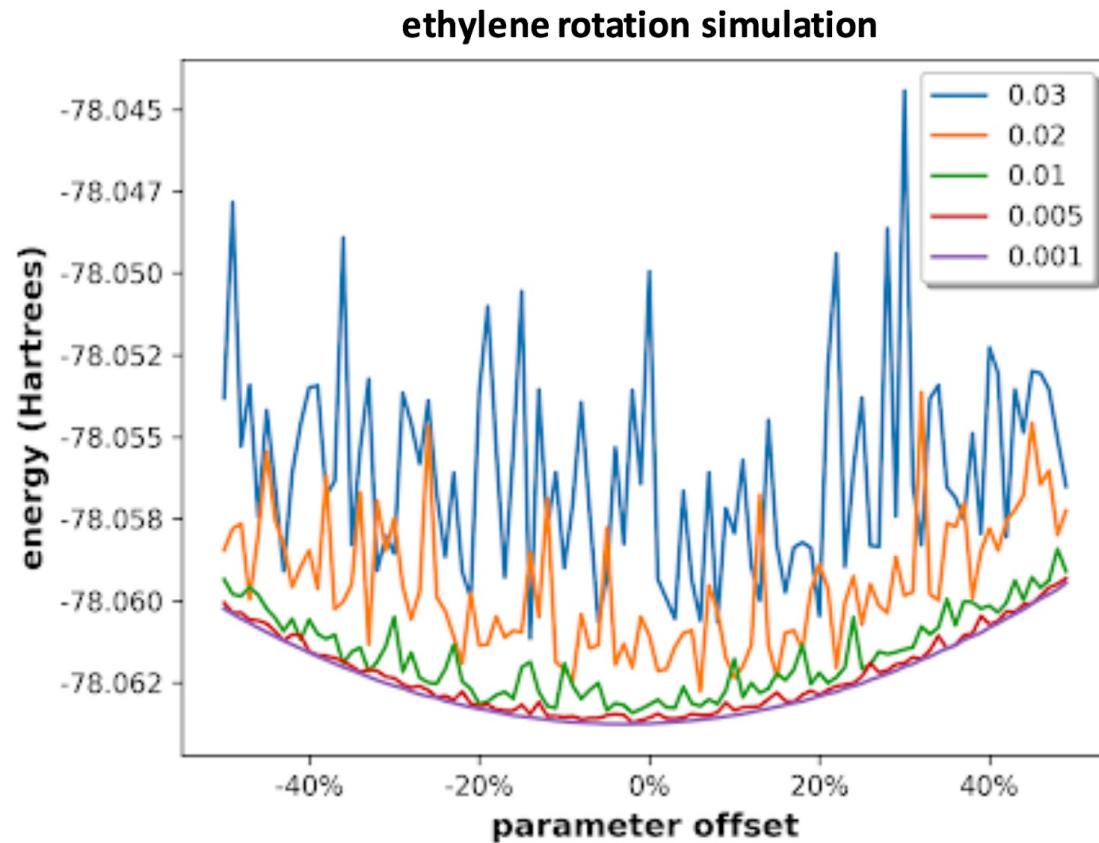


# VAQEM Tuning Overheads



<b>Bench</b>	<b>6q/f/2r</b>	<b>6q/c/2r</b>	<b>4q/c/6r</b>	<b>4q/f/6r</b>	<b>6q/c/4r</b>	<b>Li+</b>	<b>H2</b>
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# VQA Fidelity in the NISQ era



\* Classical Optimizers for Noisy Intermediate-Scale Quantum Devices QCE 2020

